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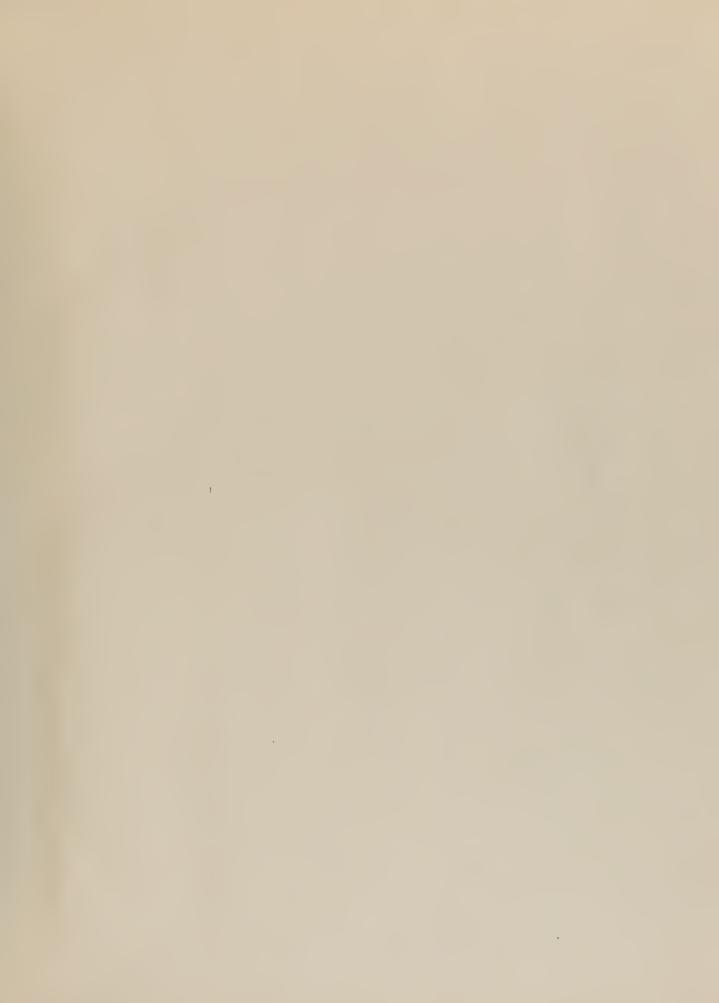
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AND DIRECTIONAL DERIVATIVES OF AN AIRPLANE BY STEADY STATE FLIGHT TESTING

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May 10, 1955

Aeronautical Engineering Report No. 302

Submitted in partial fulfillment of the requirementa for the degree of Master of Science in Engineering from Princeton University, 1955.

Thesis S 5 9 8 3

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Appreciation is due to the Armament Test Division of the Naval Air Test Jenter at Patuxent River, Maryland, for loaning the equipment used in the flight phases of this project.



SUMMARY

Navion type simplene was undertaken to determine the fersibility of using static flight test methods to find the simplest's directional and lateral static stability derivatives. It was also desired to find the variation, if any, of these serivatives with simplest velocity, power, and configuration. No attempt was made to determine any of the dynamic derivatives, since this type of testing is not designed to yield these derivatives directly.

with the aircraft instrumented to read rudder, ailaron, sideslip and roll anales, assymetric rolling and yawing moments were introduced to determine the primary and secondary control momenta. By flying straight sideslip runs with a rolling moment due to a bomb hung on the wing tip, and comparing there with runs made without the bomb, the primary alleron power is easily found. Similarly, straight didealing runs with a target tow sleave on one wing tip creating a yawing moment will lead to the rudder control power.

The secondary control moments can be firectly determined from the steady state equations of motion, or approximated from the primary moments by the use of geometric measurements of the aircraft.

Knowing the primary and decordary control moments the basic leteral and directional static stability derivatives



are found from the equations of motion in straight sideslip runs.

The flight research program clearly indicated that this type of testing was readily adaptable to this class of aircraft. The results obtained were readily repeatable on separate flights.

Definite changes in the computed derivatives were found with the programmed speed and power conditions which pointed out the necessity of conducting this type of broad coverage flight test program.



OFTERMINATION OF THE STATIC INTERAL

AND DIRECTIONAL DERIVATIVES OF AN

ARPLENE BY STEADY STATE FLIGHT PESTING

INTRODUCTION

towards the use of flight testing as a means of obtaining or checking the stability derivatives of airplanes. The high cost and doubtful accuracy of results obtained from large scale, high sneed wind tunnels has given impetus to this means of testing. It is the purpose of this investigation to determine the feasibility of applying some of the recently developed methods of obtaining stability derivatives to a light simplane.

To deduce an airplane's aerodynamic characteristics from a given flight test, it is usually recessary to analyze the response of the airplane to its various controls. The major methods now in use deal with the dynamic response of the airplane to its controls by either steady oscillation techniques or by transient response techniques. However, certain of the lateral stability derivatives can be obtained from non-dynamic steady responses to the airplane's controls.



fairly obvious. Dynamic response techniques normally require extensive instrumentation to measure the rapid motions of the airplane. The accuracy of any determination is therefore a function of the accuracy of the instrumentation and a knowledge of the airplane's mass and complicated inertia characteristics. Steady, non-oscillatory response techniques are not susceptible to many of the inherent difficulties experienced in dynamic testing. Therefore, if the airplane is not severely limited in endurance, many of the lateral derivatives can be obtained with greater accuracy and at much less cost by these means.

In this report, the methods for obtaining and analyzing flight test curves for the static lateral stability derivatives are discussed. In particular, it deals with methods of obtaining alleron power, C_{15} , rudder power, C_{n60} , secondary control moments and forces, C_{n50} , and C_{y50} , directional stability, C_{n6} , dihedral effect, C_{16} , and side force derivative, C_{y6} . The parameters are determined at varying speeds, power, and aircraft configurations to ascertain what variations occur.

The investigation was conducted during the spring of 1955 by Figure ant R. P. Smith, USN and



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Lieutenant I. T. Vogt, Jr., USN, while studying under the Department of Aeronautical Engineering of Princeton University, Princeton, New Jersey.

DIRCUSSION OF THRORY

The equations of motion of airplane lateral dynamics, using stability (wind) axes, are

In confucting steady state lateral flight testing, where $\beta = \ddot{\psi} = \dot{\phi} = \dot{\phi} = 0$, it is convenient to use the time derivative rather than DY, the non-dimensional yaw rate. Imposing the steady state conditions, the equations of motion become

$$C_{y\beta}\beta - C_{L}\frac{v}{9}\psi + C_{L}\phi + C_{y\delta_{n}}\delta_{n} = 0$$
 (a)

$$C_{\ell p} \beta + C_{\ell n} \frac{b}{2V} \dot{\psi} + C_{\ell \delta_n} \delta_n + C_{\ell \delta_n} \delta_n = 0$$
 (b) (2)

$$C_{mp} \beta + C_{mn} \frac{\delta}{RV} \dot{V} + C_{m\delta_n} \delta_n + C_{m\delta_a} \delta_a = 0$$
 (c)

In these equations there are five variables $(\beta, \psi, \phi, \delta_a, \delta_a)$.

In steady state flight testing methods particular



variables are eliminated by special flight manuevers. The three possible manuevers are the perfect turn (G=0), the straight sideslip $(\not\!\!\!\!/=0)$, and the skidding turn $(\not\!\!\!/=0)$.

The perfect turn and skidding turn maneuvers are primarily used to determine the damping derivatives ${\tt C_{nr}}$ and ${\tt C_{lp}}$, and the cross derivatives ${\tt C_{lr}}$ and ${\tt C_{np}}$. These tests were not conducted.

For the straight sidealip maneuver, the equations (2) reduce to the following:

$$C_{\gamma\beta} B + C_{L} \phi + C_{\gamma\delta n} \delta_{n} = 0 \qquad (a)$$

$$C_{\ell\beta} B + C_{\ell\delta n} \delta_{n} + C_{\ell\delta n} \delta_{n} = 0 \qquad (b) \qquad (3)$$

$$C_{n\beta} B + C_{n\delta n} \delta_{n} + C_{n\delta n} \delta_{n} = 0 \qquad (c)$$

The simplane was instrumented so that the variables β, ϕ , δ_{ν} and δ_{ν} could be recorded and the coefficient c_L determined.

The secondary control moments are expressed in terms of the primary moments as follows:

$$C_{y\delta r} = K_1 C_{m\delta r} \qquad K_1 = -\frac{b}{\ell l r} \qquad (4)$$

$$Cl_{\delta n} = K_2 C_m \delta_n$$
 $K_2 = -h_m/l_m$ (5)

$$C_{m_{\delta\alpha}} = K_3 C \ell_{\delta\alpha} \tag{6}$$

where b is the wing span, l_{v} is the horizontal distance from the airplane's c.g. to the centroid of the vertical tail and h_{v} is the vertical distance from the airplane's



X axis to the centroid of the vertical tail.

Rewriting the equations (3), the final working form was obtained.

$$C_{YB} \beta + C_{L} \phi + K_{I} C_{N\delta r} \delta_{r} = 0 \qquad (a)$$

$$C_{LB} \beta + C_{L\delta a} \delta_{a} + K_{2} C_{N\delta r} \delta_{r} = 0 \qquad (b) \qquad (7)$$

$$C_{NB} \beta + C_{N\delta r} \delta_{r} + K_{3} C_{L\delta a} \delta_{a} = 0 \qquad (c)$$

To determine the primary control moments, two known torques were applied to the aircraft and the control movement recessary to overcome this torque was easily converted to control power. To determine C_{152} , the rolling moment due to aileron, a known weight was hung on the left wingtip. This introduced a known rolling moment coefficient

$$Ce_a = \frac{Wa \cdot 3}{9 \cdot 5b} \qquad (8)$$

The yawing moment due to serodynamic drag of this weight was calculated to be negligible.

In wings level flight ($\phi = O$), the rolling equilibrium equation from (7b) and (8) is

Cla β + Clsa δ a + K_2 Cnsa δ a + Cla = O (9) At zero sideslip then, the ailerons must be deflected a larger angle with the introduction of C_{1a} . For a first appreximation the secondary control moment, K_2 Cnsa δ a was assumed equal to zero. Thus the sileron control power was

$$Ce_{\delta a} = -\frac{Ce_a}{\Delta \delta a} \tag{10}$$

The rudder control nower Cn & was determined



by introducing a known yawing moment about the airplane's Z exis and balancing it by rudder deflection.

Using a strain gage instrumented tow target sleeve attached to the wing tip, the known yawing momentwas $C_{ma} = \frac{O_r \cdot M}{gSb}$ (//)

The yawing equilibrium equation became

$$C_{mp}\beta + C_{ms_1}\delta_r + K_3 C_{ls_a}\delta_a + C_{ma} = 0 \qquad (12)$$

Test data at zero mileslip, sleeve on and off, gave the difference of rudder deflection required. Considering as a first approximation that the aileron adverse yaw,

K3 C4 & , was zero, the rudder power was

$$C_{m s_n} = -\frac{C_{m a}}{\Delta s_n} \tag{13}$$

Returning to the assymetric weight test, the difference of rudder angles required for trim between weight on and off is due to the yawing mement of the edditional dileron deflection. From equation (7c)

can now be solved for K3, thus:

$$K_3 = -\frac{C_{m_{Sa}}}{C_{P_{Sa}}} \cdot \frac{\Delta}{\Delta} \frac{\delta_a}{\delta_a} \tag{14}$$

Iteration of the coefficients \mathcal{I}_{15a} , \mathcal{I}_{n5a} and of Kz was used to obtain the most accurate answers for the data collected by the following equations:

$$C_{sa} = \frac{-C_{la} - K_2 C_{msn} \Delta \delta n}{\Delta \delta a} \tag{15}$$

$$C_{m\delta n} = \frac{-C_{m\alpha} - K_3 C_{p\delta\alpha} \Delta_{\delta\alpha}}{\Delta_{\delta\alpha}} \tag{16}$$

Finally, the three geconiary control moments



Cyor, C_{152} and C_{n52} can be obtained from equations (4), (5), and (6).

Knowing the primary and secondary control moment coefficients, the static lateral stability derivatives, $C_{y\beta}$, $C_{l\beta}$ and $C_{n\beta}$, were determined from the straight sideslip equations (7a), (7b), and (7c). The slopes of the flight test data curves through zero sideslip are used in the following equations to determine the static lateral and directional derivatives.

$$C_{\gamma\beta} = -C_L \frac{\partial \phi}{\partial \beta} - K_i C_{n\delta n} \frac{\partial \delta r}{\partial \beta} \qquad (a)$$

$$C_{\ell\beta} = -C_{l_{\delta\alpha}} \frac{\partial \delta\alpha}{\partial \beta} - K_2 C_{m\delta n} \frac{\partial \delta\alpha}{\partial \beta} \qquad (b) (17)$$

$$C_{mp} = -C_{ms_n} \frac{\partial s_n}{\partial \beta} - K_3 C_{ls_n} \frac{\partial s_n}{\partial \beta} \qquad (c)$$

EQUIPMENT AND PROCEDURES

The test vehicle used to obtain flight data was a Ryan Navicn, N5113K. This is a four-place transport powered by a 205 HP Continental engine. The aircraft was standard in configuration except for the modifications made for these tests, and is pictured in Figs. 1, 2 and 3.

In order to mount the equipment required to place known rolling and yawing moments on the aircraft, two steel lugs were fastened to the outermost stiffening rib of each wing. To each of these a standard U. S. Navy Mark 8 homb shackle was attached. These shackles are manually operated



and were activated by steel cables led through the wing to the cockpit (Fig. 3).

A boom with a yaw vane attached was mounted so as to extend forward from the left wingtip lugs (Fig. 1).

Movement of the vane energized an autosyn transmitter mounted within a streamlined shape. This boom was sufficiently long so that it was logical to assume that the vane was not affected by the aircraft pressure field. Another boom extended aft from the right wing tip lugs. This was used to support the equipment required to give a known yawing moment.

Fig. 3 shows this arrangement.

a "homb", actually a streamlined scane made of stock steel, was carried on each north shackle for takeoff. Although these bombs weighed approximately 80 nounds each, no undue stress concentration was noticed during takeoff or during any maneuvers. After takeoff, the right bomb was dropped, and a series of tests made with the known weight (7% lbs., 5 ozs.) on the left wingtip. (All takeoffs and landings were made with symmetrical loads since there was some doubt if the sincraft would have sufficient sileron power at low speeds in the unbalanced condition. It is felt that this was unnecessary.) Then the homb on the left wingtip was dropped and the same tests made in the clean configuration. In this way, duplication of etmospheric conditions was obtained.



To determine $C_{n,\delta,\epsilon}$, a standard U. 3. Navy Mark 23, Mod C, O foot tow target sleeve was towed behind the right wingtip. Crisinally, takeoffs were made by stretching 450 feet of nylon line, with the sleeve attached, ahead of the airplane. A maximum performance takeoff was made and the target "snatched" into the air. Power limitations of the aircraft coupled with the roughness and short length of the field precluded any successful "snatches" without approximately 10 knots of headwind.

These limitations finally caused a redesign of the system to that shown in Fig. 2. In this system, the target was fastened to the rear of the fuselage with 150 feet of line and the remainder of the line looped from the tail to the wingtip. After takeoff and climb out, the tail attachment point was released and the target supported by the wingtip.

Some difficulty was experienced on several test flights when the tow target started to oscillate and rotate. The only apparent cause was that the target was in the wing vortex trail. By placing a five pound weight on the target apport ring, this difficulty was alleviated.

To measure the drag of the target a strain gage unit was designed and placed directly aft of the boom. Electrical wires were led through the wing structure and readings made on a Baldwin SR-4 strain gage box in the cookpit. Immediately aft of the strain gage a "pelican" type



release hork was attached with an activating on le led into the cockpit. The target was released prior to landing and on all unsuccessful "anatches". Fig. 3 shows the right wingtip arrange ent. It was found absolutely essential to have a dependable meaning in the line to take out any twist caused by rotation of the target in the air. Once again the same tests were run in the clean configuration in order to duplicate atmospheric conditions.

mitter was mounted on the sudder surface and another on the aileron control cable. This equipment was around colibrated. It is interesting to note that only differences and slopes of all measured quantities were used in the computations. Therefore it was not recessary to determine accurately the mero points of control deflections or sidealing indications. A standard double needle autosyn receiver-indicator was mounted in the cockpit and with suitable step-up pulleys, large indicator deflections were obtained for small control deflections.

Since these tests were being conducted concurrently with another series on the aircrift, sidealip indications were obtained by converting the autosyn transmitter output to a direct current voltage. Readings were then made on a direct current voltage.

A standard inclinometer was mounted in the cockpit



perpendicular to the roll axis of the aircraft in order to read roll angle. With proper shock mounting to damp out high frequency vibrations, this gave very satisfactory results.

Even though the primary purpose of this investigation was to determine the feasibility of obtaining certain of the lateral and directional atability derivatives by static flight test means, the variation of these derivatives with aircraft speed, power, and flap deflection was also desired. To accomplish this end, seven series of tests were mode. With power for level flight, tests were made at 80, 100, and 120 miles per hour. For the three tests made at each speed, i.e. assymetric weight, assymetric drag, and clean, the engine speed was held constart, 1800 rpm for 80 mon, 1900 rpm for 100 rph, and 2000 rpm for 120 mph. The same series of tests were then conducted at 80, 100 and 120 noh with maximum continuous power applied. For this aircraft maximum continuous power is list d as 25 inches manifold presoure and 2300 rpm. In these tests of course, the aircraft climbed. In addition, a series of tests were made at maximum continuous power with full flap deflection. Results of all tosts are shown on Fig. 4 through Fig. 17.

In all configurations, the data desired was \mathcal{S}_{ω} , \mathcal{S}_{ω} , and ϕ at various angles of sidealin, ρ . The bast method to



obtain data was to deflect the rudder and stop the aircraft from turning by deflecting the aileron. Then readings were taken. In addition drag readings from the strain gage box were taken for the runs when the target was being towed. Straight flight was maintained by constant reference to the directional gyro.

DISCUSSION OF RESULTS

The data obtained from the seven different test conditions was plotted in Figs. 4 through 17, and results computed from these curves were listed in Table II. As the analysis of results was identical in all seven configurations, only the power for level flight run at 100 mph will be discussed in detail.

At V_1 = 100 mph, q was found using the aircraft position error charts to be 27.7 lbs. per sq. ft., C_1 was .519 and by was 2.3 ft.

From equation (8), $C_{1a} = -.00769$. Equation (11) gave a value for $C_{na} = .00971$.

Using equation (10) and an aileron deflection at zero sideslip from Fig. 6 of 3.6° , the aileron control power $\text{Ci}_{k} = -.124$.

From e wation (12) and Fig. 7, the first approximation of the rudder control power was $C_{n_{s_2}} = -\frac{200971}{4.8/s_{23}} = -.116$.



Now the proportionality factor K_3 could be computed by equation (13), using the control deflections at zero sideslip thus: $K_3 = -\frac{-.1/6}{./24} \cdot \frac{-.4}{3.6} = -./04.$

Iteration of these coefficients by equations (14), (15), and (13) produced the following final values:

$$c_{1}c_{n} = .124$$
 $c_{n}c_{n} = -.119$
 $c_{n}c_{n} = -.107$

From equations (4), (5) and (6) the three secondary control moments were found to be

$$C_{ysn} = -.236$$
 $C_{1sn} = .0166$
 $C_{nsn} = -.0138$

Finally, using the roll angle, rudder angle and eileron angle slopes from Fig. 6, the static lateral derivatives for $V_1 = 100$ mph were determined from equations (17a), (17b) and (17c).

$$C_{yp} = -.546$$
 $C_{1p} = -.0865$
 $C_{rp} = .144$

variations in the computed values of the primary control nowers, secondary control powers and stability derivatives with the change in speed and power conditions. These variations are to be expected and the influencing factors



are detailed below. The limiting accuracy in these calculations was felt to be the inherent inaccuracy involved in measuring and recording flight test data, then subsequently fairing curves and attempting to read control deflection differences closer than 0.1°. In particular, the aileron deflection measuring system was attached at the control column and thus no accurate account could be taken of cable stretch even though attempts were made to "load" the ailerons during the ground calibrations.

Table II and Fig. 18 show that $C_{1/2}$ decreases as speed increases. Since alleron control cable stretch would increase as dynamic pressure increased, this could partially contribute to the reduction in alleron power at higher speeds. The normal lessening of alleron power as $C_{1/2}$ decreases and any wing twist at higher speeds would also account for some of the noted reduction in $C_{1/2}$.

From Table II and Fig. 18 C_{nga} is seen to decrease with an increase in velocity. Since the rudder lies within the slingtness, this would be expected. As forward speed is increased, the effect of the slipstness decreases, and less force is exerted by the rudder per degree of deflection.

 C_{15A} is a function of C_{n5A} and might therefore be expected to decrease as velocity increases. However, as velocity increases the angle of attack decreases. This will increase h_V and from equation (5), C_{15A} would be increased.

The sileron adverse yaw, Cnsa is seen to decrease



with speed. Aileron adverse yew is partially the result of the increase in induced drag which accompanies the increase in lift of the wing when the aileron is deflected downward. Since induced drag is a function of ${\tt C_L}^2$ it is expected that it would tend to decrease as velocity increases.

The side force derivative, C_{yp} , should theoretically stay constant with charges in speed. The minor variations noted in Table II and Fig. 19 could possibly be caused by charges in the interference and sidewast effects of the fuseloge and slipstmenm as speed in charged. This would affect the angle of attack of the vertical tail differently at the lifferent speeds and power conditions.

Directional stability, $C_{n\beta}$ is almost explusively determined by the vertical tail. Since the vertical tail lies within the alipstream, $C_{n\beta}$ would be expected to decrease as alipstream becomes less effective, i.e. as appeal increases. This was noted in Table II and Fig. 19. Comparing $C_{n\beta}$ at the same speed and different power settings, Table II shows that the directional stability is reduced alightly, as power is increased. This might be explained by the fact that tractor propellers are destabilizing as the power is increased.

An expected, dihedral effect, $\mathcal{I}_{1\beta}$, is seen to charge very little with velocity. A possible reason for the small decrease in $\mathcal{I}_{1\beta}$ as power is increased at constant speed is that the added alignment five to the power acts over one wing more than the other as the sincreft is sidealined.



This introduces a rolling mement which would decrease the magnitude of Cla.

It is difficult to explain the variations seen in Table II and on Figs. 18 and 19 in the computed values of the several derivatives when the flaps were deflected. Some of the variations can be rationalized however, and these will be discussed. Since the flaps tend to interfere with the flow of the propeller slipstream over the vertical tail, the reduction in $C_{n_{1}}$, is to be expected even though the speed is lower. The minor variation of C_{1} from what would be expected at low speed is not explainable.

The flap hinge line on the test aircraft was swept forward a small amount. This would partially account for the increase in the magnitude of $C_{y_{\mathcal{S}}}$ and the decrease in $C_{1_{\mathcal{S}}}$. The interference of the deflected flaps with the slipstream would also indicate a decreased value of $C_{n_{\mathcal{S}}}$ from clean condition.

A refir ment in the method of solution for primary and secondary control moments could have been used if an accurate determination of yawing moment of the weight and rolling moment of the sleeve had been made. In this project, bomb drag was calculated and found to be negligible. Rolling moment of the sleeve could be found if an accurate determination of the angle between the tow line and the aircraft's X axis (Mcrizon) were made.

Then from equation (3)(b) and (8), repeated here



$$Cl_{\beta}\beta + Cl_{\delta\alpha}\delta_{\alpha} + Cl_{\delta\alpha}\delta_{r} = 0$$
 (3b)

$$Cla = \frac{Wa \cdot 4}{95b} \tag{8}$$

two difference equations at zero sideslip could be written:

The first approximation of C_{1s} Δs_{∞} would give an identical answer for C_{1s} as the method used in this report. However, with an accurate control deflection measuring system and the above mentioned moments, it was felt that simultaneous solution of these equations would provide a more accurate determination of C_{1s} which would not depend on the questionable measured values of h_v and h_v .

Similarly equations (3)(c) and (11) can be written as difference equations at zero sideslip.

Construction of these equations gives
$$C_{nst}$$
 and C_{nsa} without the

iteration procedure proviously used.

It was felt that state flight testing procedures are easily accurate enough to justify this method of solution.



CONCTUSIONS

The flight testing required for this method of determination of the static lateral and directional stability derivatives is relatively easy to perform.

The primary and secondary alleron and rudder control moments are determined directly by the flight tests.

Instrumentation necessary to obtain required flight test data is not complex and is readily available.

Reduction of flight test data and the computations necessary to extract the stability derivatives are fast and straightforward.

The dir ctional stability and effective dihedral were found to charge markedly with aircraft velocity. For the aircraft tested, there was a distinct decrease in $C_{n,\beta}$ and $C_{1\beta}$ has speed increased. Therefore, it is recommended that an aircraft always be tested at various speeds and in its different configurations.

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TABLE I

DESCRIPTION OF SYMBOLS

- V Airplane velocity f.p.s.
- S Wing area (sq. ft.)
- b Wing span (ft.)
- ly Length c.g. to vertical tail centroid (ft.)
- hv Vertical toil centroid to X axis (ft.)
- OI, Airplane Lift coefficient
- q Dynamic pressure (1bs./sc. ft.)
- 3v Side force coefficient Y/qs
- C1 Rolling moment coefficient L/qsb
- Cn Yawing moment coefficient N/qsb
- M Airplene relative density m/ssb
- D Differential operator da(t/2)
- Bideslip angle
- Y Yaw angle
- ø 3ank angle
- So Rudder angle
- δ_∞ Aileron angle (average)
- Cya Side force derivative 204/28 (per radian)
- Cra Directional stability derivative dem/da (per radian)
- Cla Dihedral effect 202/03 (per radian)



TABIS II

	Tevel	Flight Power Maximum Continuous Power				ower	
	1800RPM	1900RPM	2000 (PM	2300RPM	2300RPM	2300 RPM	2300RPM
Vi	80	100	150	80	. 100	120	70
q	17.7	27.7	37.9	17.7	27.7	37.9	1.3.6
Clasomb	01204	00769	00567	01204	00769	00567	01568
Cna Sleet	.01150	.00971	.00897	.01150	.00971	.00897	.01060
CL	.811	.519	.390	.811	.519	.390	1.06
$\Delta \mathcal{E}_{a_{ROMb}}$	4.70	3.6°	3.20	4.30	3.50	2.90	7.80
△{r cmo	1.50	0.40	0.10	1.20	0.90	0.40	0.70
Δδη 3 net	4.60	4.80	4.80	4.90	5.60	5.70	5.5°
Δίς Sleet	C.80	1.10	0.80	0.80	0.80	1.00	0.60
Clsa	.15?	.124	.101	.164	.129	.100	.115
Cnsa	151	119	107	140	105	0925	112
K3	318	107	032	->37	209	124	087
Clsa	.0130	.0166	.0166	.0119	.0141	.0143	.0152
^C nsa	0561	0138	0032	0388	0270	0124	0100
Jysn	.291	.236	.203	.266	.500	.176	.213
do/88 -	.39	.58	.87	.44	.61	.87	.46
der/ap	.98	1.14	1.30	1.17	1.16	1.39	1.28
·dsa/dp	.47	.55	.57	.48	.49	.56	.13
Cyp	616	546	595	671	551	560	760
Clp	0905	0865	0822	0957	0814	0736	0344
onp	.181	.144	.141	.180	.140	.118	.144



Fig. 1 Test Aircraft Showing Bombs





Fig. 2 Test Aircraft Showing Tow Target Sleeve



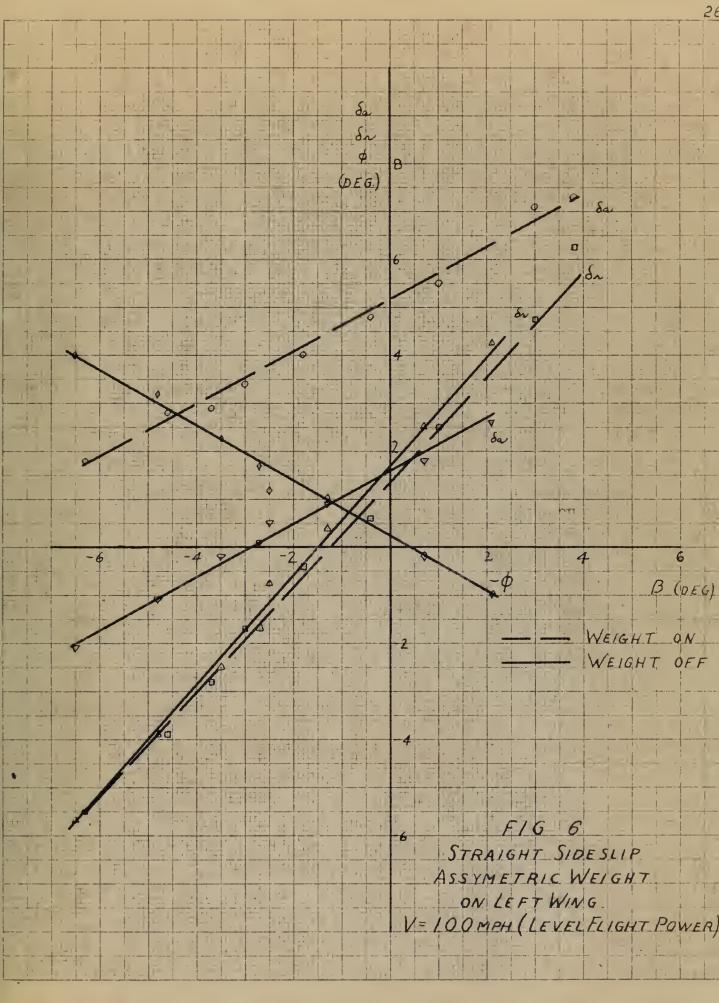


Fig. 3 Detail of Right Wingtip

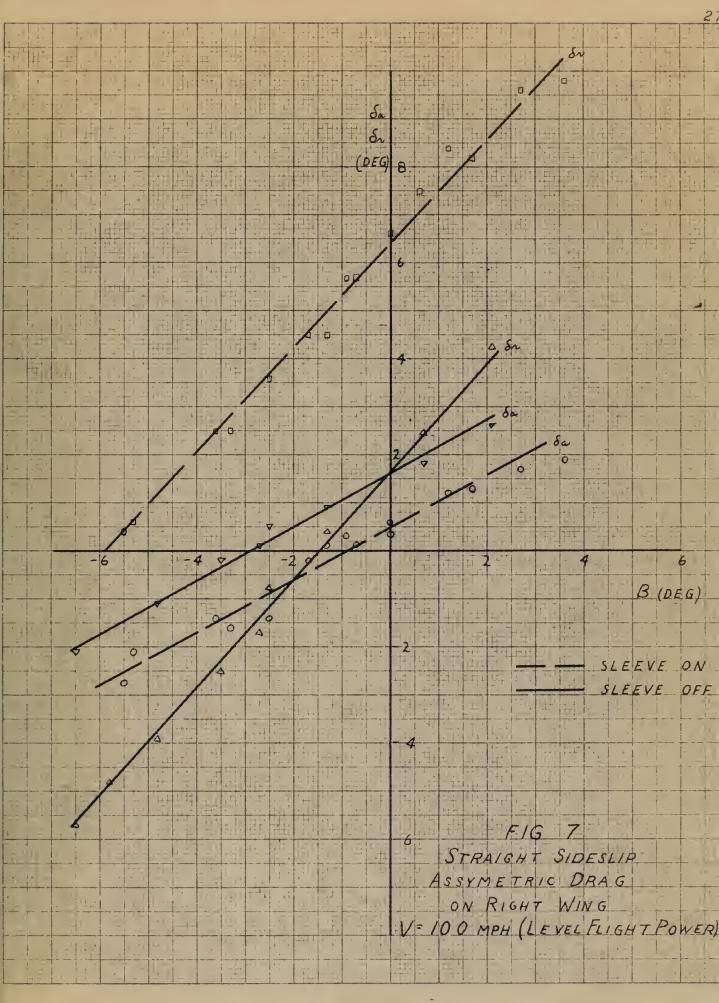




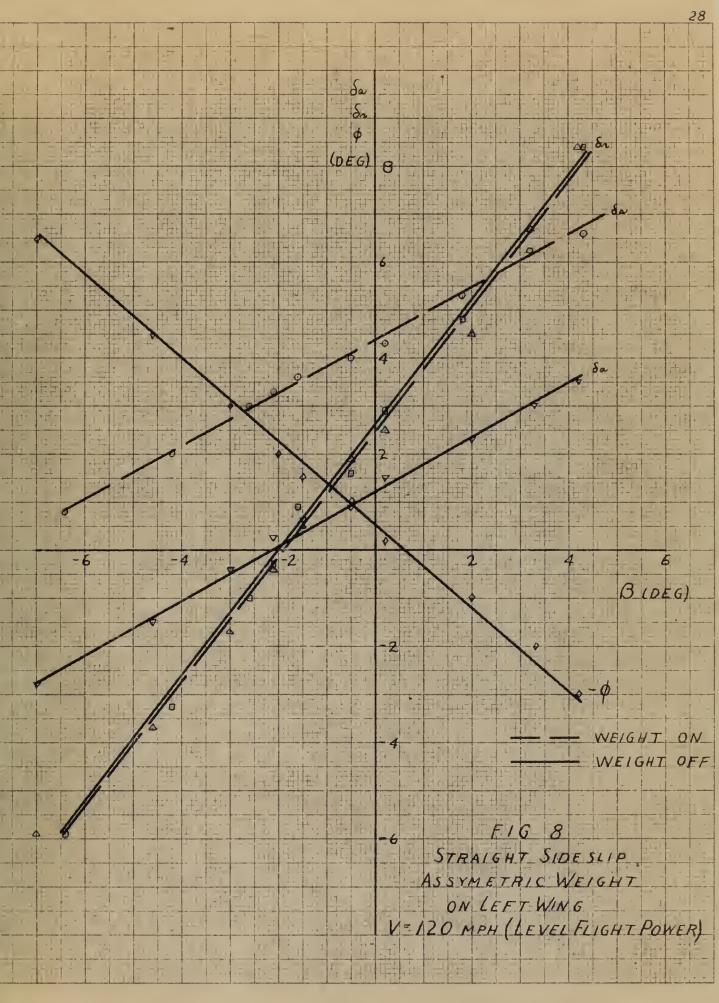






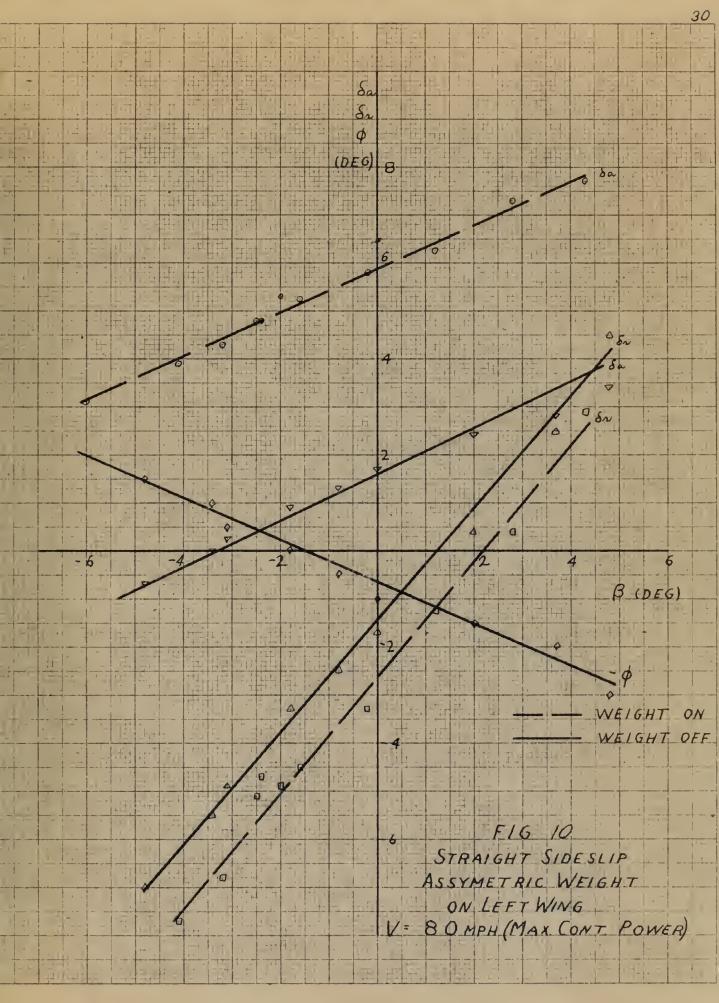




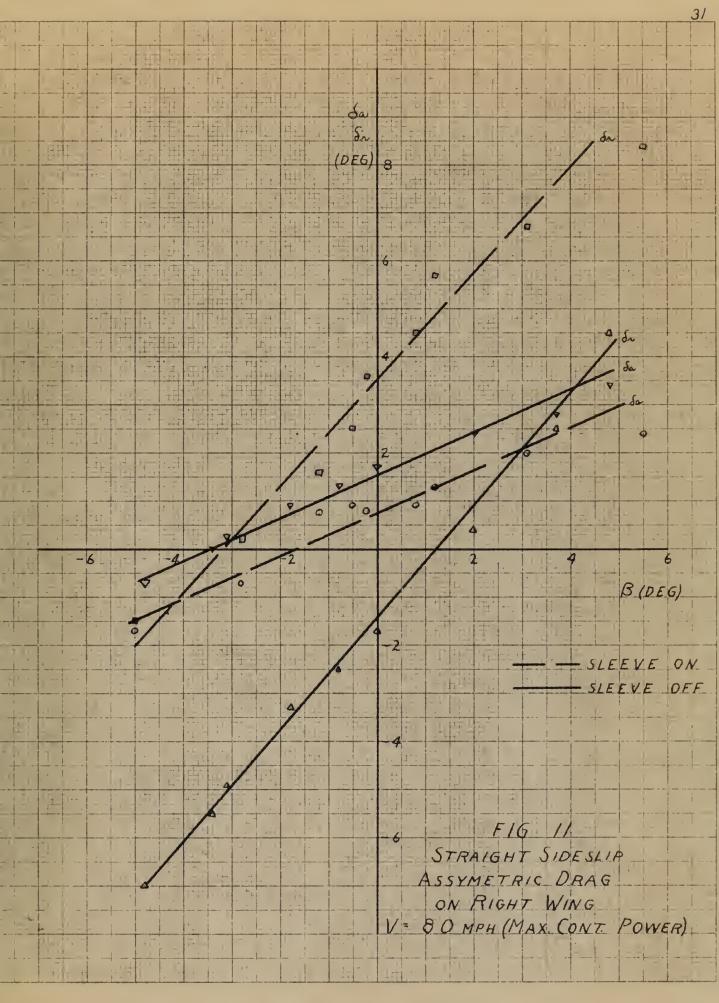






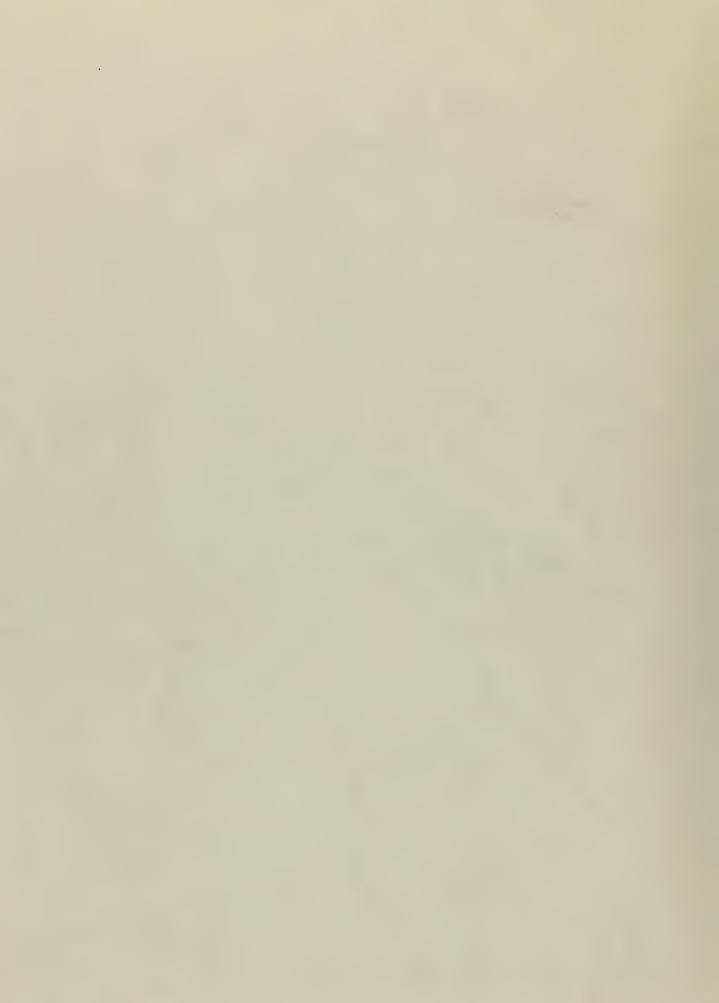


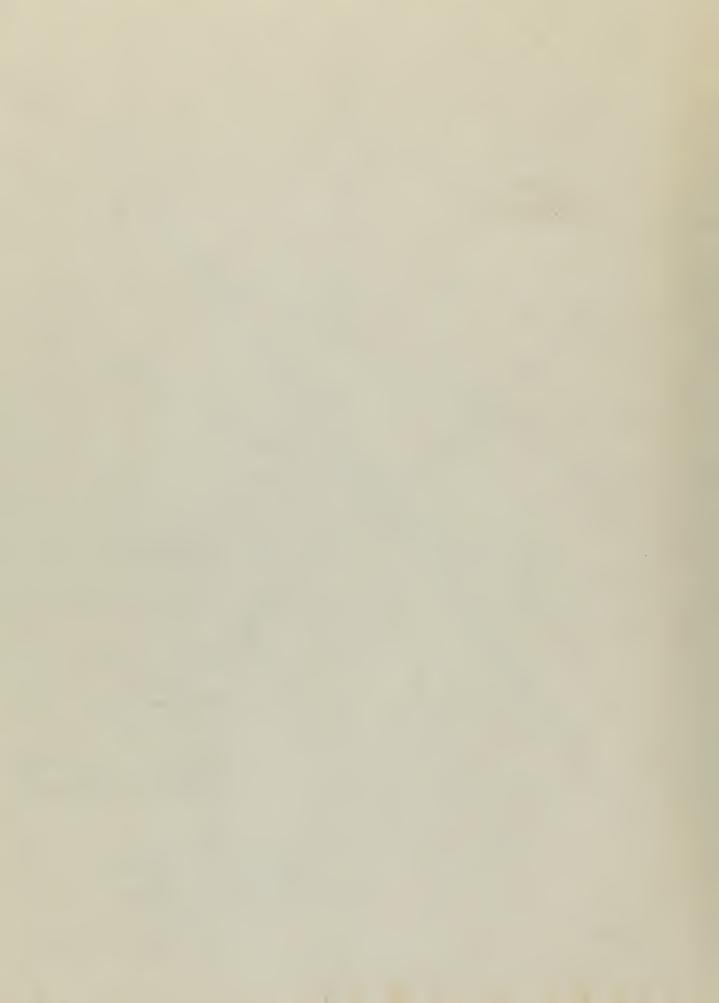






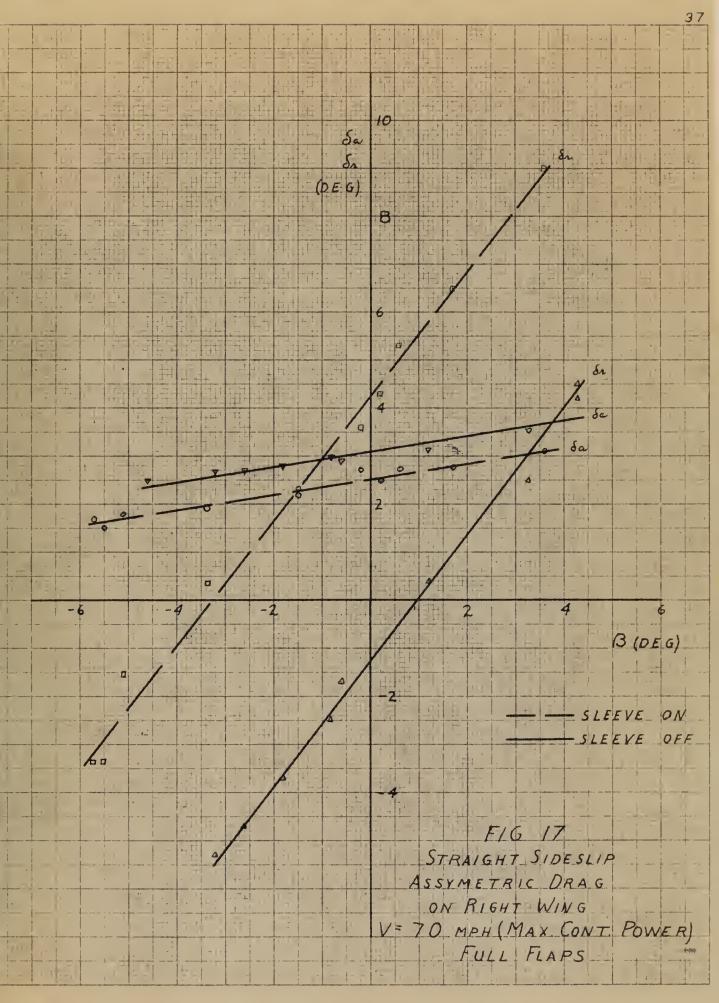






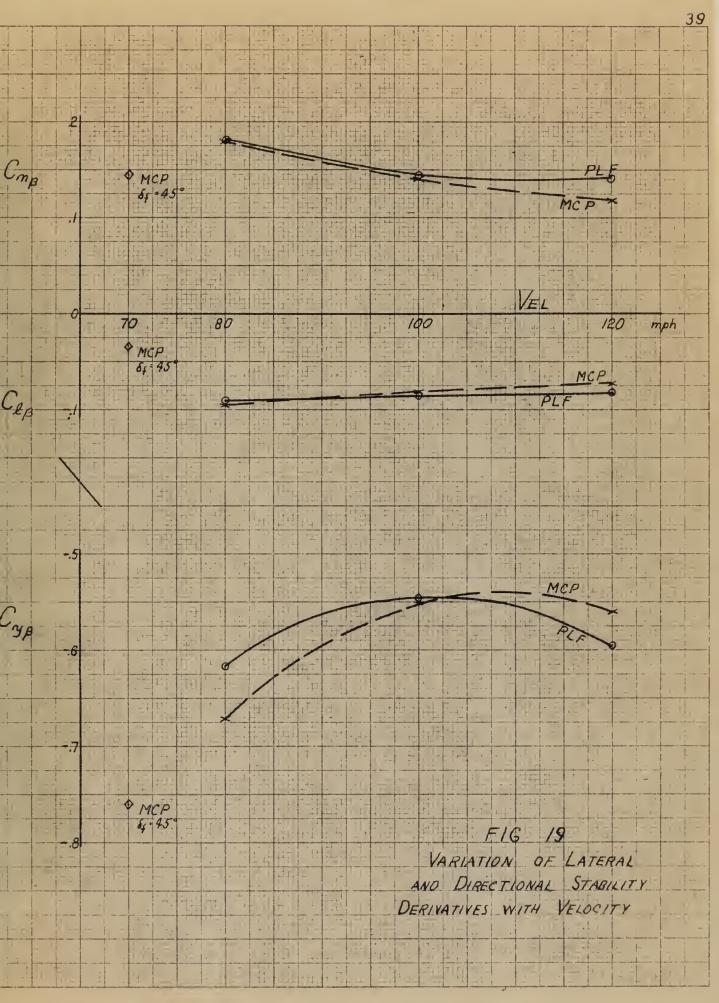






















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